

# Industrial Organization

## Problem Set #1 Solution

Universidade Nova de Lisboa  
Faculty of Economics  
Fall 2008

**Instructor:** Vasco Santos  
**Grader:** David Henriques

### 1 Concentration and Volatility Measures

a. (10 points)

Year	Firms						Concentration Index		
	1	2	3	4	5	Other(s)	$C_4$	$\inf H$	$\max H$
2000	40%	15%	15%	15%	15%	0%	<b>0.85</b>	<b>0.25</b>	<b>0.25</b>
2006	45%	11%	11%	11%	11%	11%	<b>0.78</b>	<b>0.2509</b>	<b>0.263</b>

• **Year 2000**

$$C_4 = \sum_{i=1}^4 s_i = 0.4 + 0.15 \times 3 = 0.85 \quad (0.5 \text{ points})$$

$$\inf H = \sum_{i=1}^5 s_i^2 = 0.4^2 + 4 \times 0.15^2 = 0.25 \quad (0.5 \text{ points})$$

$$\max H = \inf H = H = 0.25. \quad (0.5 \text{ points})$$

• **Year 2006**

$$C_4 = \sum_{i=1}^4 s_i = 0.45 + 0.11 \times 3 = 0.78 \quad (0.5 \text{ points})$$

$$\inf H = \sum_{i=1}^n s_i^2 = 0.45^2 + 4 \times 0.11^2 = 0.2509 \quad (1 \text{ point})$$

$$\max H = 0.2509 + 0.11^2 = 0.263. \quad (1 \text{ point})$$

According to the four-largest firms' concentration index, in the year 2000 the industry was more concentrated than in the year 2006. (1 point)

According to the Hirschman-Herfindahl concentration index the conclusion is reversed, i.e., the industry was more concentrated in 2006 than in 2000. Notice that  $\inf H_{2006} = 0.2509 > 0.25 = \max H_{2000}$ . (1 point)

**Adelman's equivalent number (EN)**, is the number of equal-sized firms that yields a given level of market concentration in the Herfindahl index. (0.5 points)

- Year 2000 equivalent number,  $EN_{2000} = \frac{1}{H_{2000}} = \frac{1}{0.25} = 4.0$ . (0.5 points)
- Year 2006 equivalent number range,

$$\frac{1}{\max H_{2006}} \leq EN_{2006} < \frac{1}{\inf H_{2006}} \iff \frac{1}{0.263} \leq EN_{2006} < \frac{1}{0.2509}$$

$$\iff 3.8023 \leq EN_{2006} < 3.9857. \quad (1 \text{ point})$$

### Instability index

$$I = \frac{1}{2} [|0.45 - 0.4| + 4 \times |0.11 - 0.15| + |0.11 - 0.0|] = 0.16. \quad (2 \text{ points})$$

b. (10 points)

i)

$$C_4 = \sum_{i=1}^4 s_i = 0.6 + 0.1 + 0.05 + 0.05 = 0.8 \quad (1 \text{ point})$$

$$H = \sum_{i=1}^8 s_i^2 = 0.6^2 + 0.1^2 + 6 \times 0.05^2 = 0.385. \quad (1 \text{ point})$$

ii)

$$\hat{C}_4 = \sum_{i=1}^4 s_i = 0.6 + 0.15 + 0.05 + 0.05 = 0.85 \quad (1 \text{ point})$$

$$\hat{H} = \sum_{i=1}^7 s_i^2 = 0.6^2 + 0.15^2 + 5 \times 0.05^2 = 0.395. \quad (1 \text{ point})$$

iii)

$$\Delta C_4 = 0.85 - 0.8 = 0.05 \quad (0.5 \text{ points})$$

$$\Delta H = 0.395 - 0.385 = 0.01. \quad (0.5 \text{ points})$$

*iv)*

$$\bar{C}_4 = \sum_{i=1}^4 s_i = 0.6 + 0.15 + 0.1 + 0.05 = 0.9 \text{ (1 point)}$$

$$\bar{H} = \sum_{i=1}^6 s_i^2 = 0.6^2 + 0.15^2 + 0.1^2 + 3 \times 0.05^2 = 0.4. \text{ (1 point)}$$

*v)*

$$\Delta C_4 = 0.9 - 0.8 = 0.1 \text{ (0.5 points)}$$

$$\Delta H = 0.4 - 0.385 = 0.015. \text{ (0.5 points)}$$

*vi)*

For the merger between 2 and 3,  $\hat{H} = 0.395 > 0.18$  and  $\Delta H = 0.01 > 0.005$ . Thus, this merger may be challenged. (1 point)

For the merger between 6, 7, and 8,  $\bar{H} = 0.4 > 0.18$  and  $\Delta H = 0.015 > 0.005$ . Hence, this merger may also be challenged. (1 point)